

## SOME IDENTITIES ON PRIME NEAR RINGS WITH GENERALIZED DERIVATION

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As a generalization of derivation the notion of generalized derivation in near ring  $N$  was introduced by Öznur Gölbası [2]. An additive mapping  $F: N \rightarrow N$  is said to be a right generalized (resp., left generalized) derivation with associated derivation  $d$  on  $N$  if  $F(xy) = F(x)y + xd(y)$  (resp.,  $F(xy) = d(x)y + xF(y)$ ) for all  $x, y \in N$ . A mapping  $F: N \rightarrow N$  is said to be a generalized derivation with associated derivation  $d$  on  $N$ . The purpose of the present paper is to obtain the commutativity of a prime near ring  $N$  with a generalized derivation  $F$  associated with a nonzero derivation  $d$  satisfying one of the conditions:

- (i)  $[F(x), y] = \pm y^p(x \circ y)y^q$ ,
- (ii) (ii)  $[x, F(y)] = \pm x^p(x \circ y)x^q$ ,
- (iii) (iii)  $F(x) \circ y = \pm y^p[x, y]y^q$ ,
- (iv) (iv)  $x \circ F(y) = \pm x^p[x, y]x^q$ ,
- (v) (v)  $F(x) \circ y = \pm y^p(x \circ y)y^q$ ,
- (vi)  $[x, F(y)] = \pm x^p[x, y]x^q$ ,
- (vii)  $[F(x), y] = \pm y^p[x, y]y^q$  and
- (viii) (viii)  $x \circ F(y) = \pm x^p(x \circ y)x^q$  for all  $x, y \in N$

and  $p \geq 0, q \geq 0$  are non-negative integers.

1. *Podlubny I.* Fractional Differential Equations. — Academic Press, San Diego, 1999. — 340 p.
2. *Kushnir R. M. and Yasinsky A. V.* Optimal Heating Control of Thermosensitive Rectangular Domain Under Restrictions on Stresses in a Plastic Zone // J. of Thermal Stresses. — 2010. — 33, No. 3. — P. 251–261.

**ДЕЯКІ СПІВВІДНОШЕННЯ НА ГОЛОВНИХ МАЙЖЕ КІЛЬЦЯХ З  
УЗАГАЛЬНЕНИМ ДИФЕРЕНЦЮВАННЯМ**